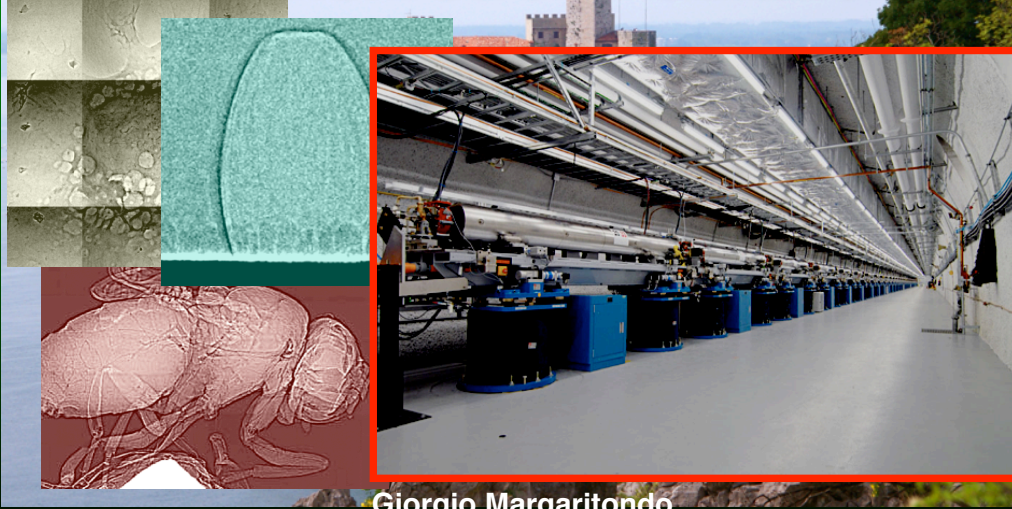


Characteristics and Properties of Synchrotron Radiation



Giorgio Margaritondo

Ecole Polytechnique Fédérale de Lausanne (EPFL)

XI Scuola di Luce di Sincrotrone - Duino 2011

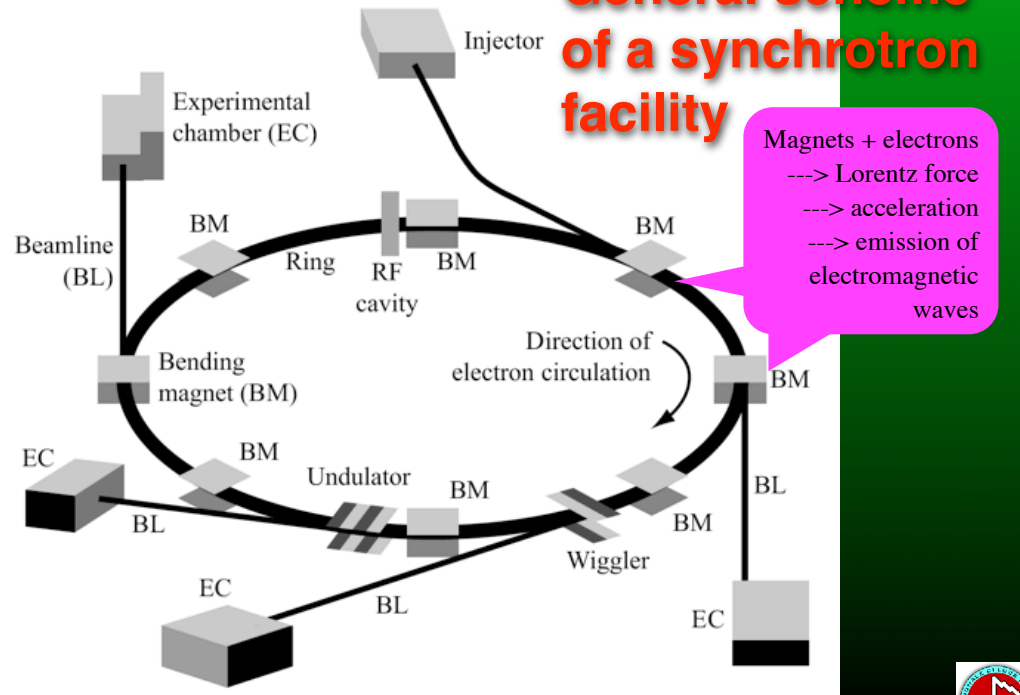


Outline:

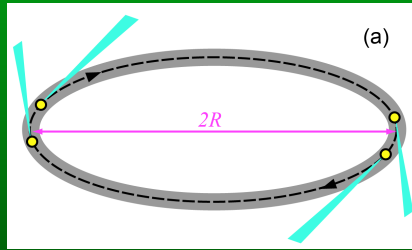
- **How to build an excellent x-ray source using Einstein's relativity :**
 - Collimation
 - Photon energy range
 - Brightness
 - Polarization
 - Undulators, bending magnets, wigglers
- **Coherent x-rays: a revolution in radiology**
- **From storage rings to free electron lasers**



General scheme of a synchrotron facility

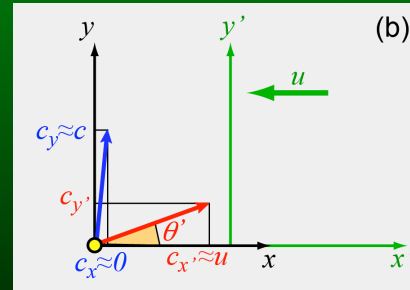


Angular Collimation:

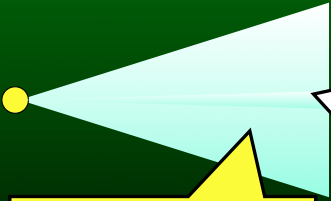


Electrons circulating at a speed $u \approx c$ in a storage ring emit photons in a narrow angular cone, like a “flashlight”: why?

Answer: RELATIVITY



But in the laboratory frame the emission shrinks to a narrow cone



Seen in the electron reference frame, the photons are emitted in a wide angular range

Take a photon emitted (blue arrow) in a near-transverse direction in the (black) electron frame, with velocity components $c_x \approx 0, c_y \approx c$. In the (green) laboratory frame the velocity (red arrow) components become $c_x' \approx u, c_y' \approx (c^2 - u^2)^{1/2} = c/\gamma$. The angle θ' is $\approx c_y'/c = 1/\gamma$ -- very narrow!!!



Fireplaces and torchlights :



A fireplace is not very effective in "illuminating" a specific target: its emitted power is spread in all directions



A torchlight is much more effective: it is a small-size source with emission concentrated within a narrow angular spread

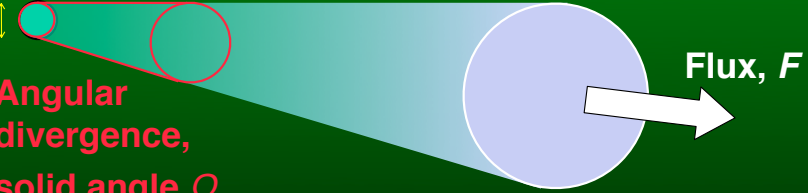
This can be expressed using the "brightness"

The “brightness” (or brilliance) of a source of light :

Source
area, $\approx \xi^2$

ξ

Angular
divergence,
solid angle Ω

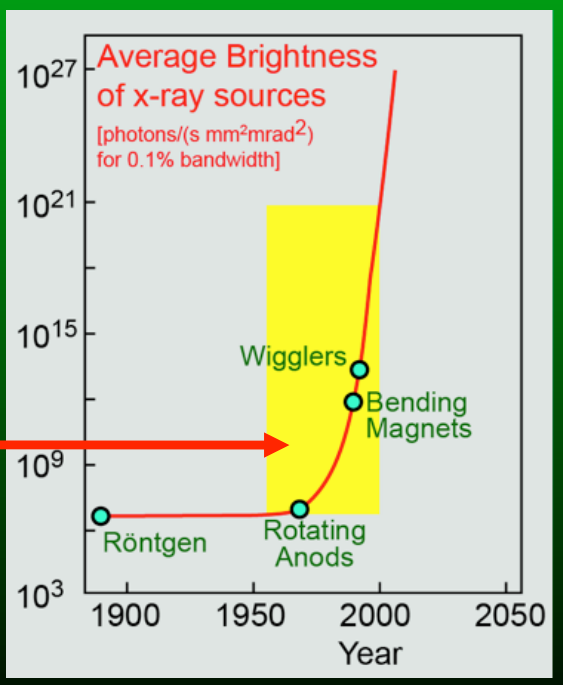


$$\text{Brightness} = \text{constant} \frac{F}{\xi^2 \Omega}$$



The historical growth in x-ray brightness/brilliance

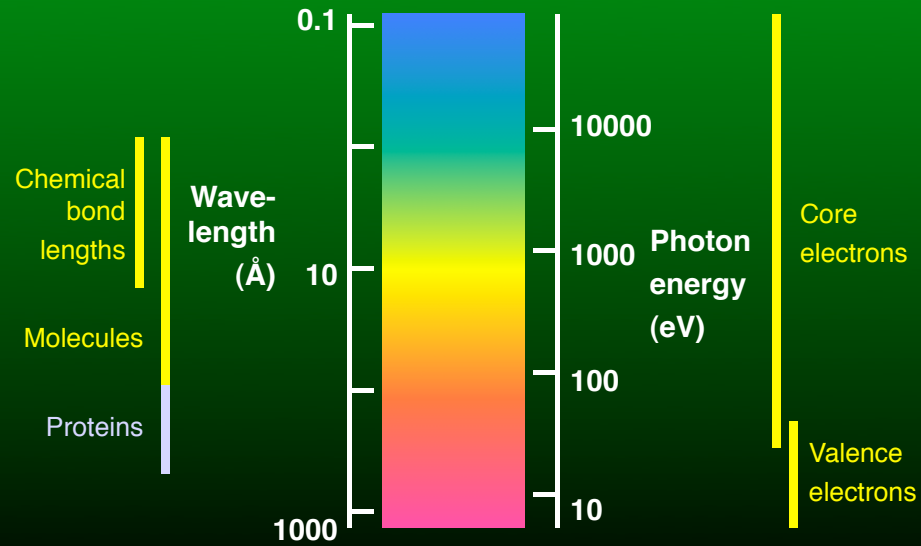
Between 1955 and 2000, the brightness increased by more than 15 orders of magnitude... whereas the top power of computing increased "only" by 6-7 orders of magnitude

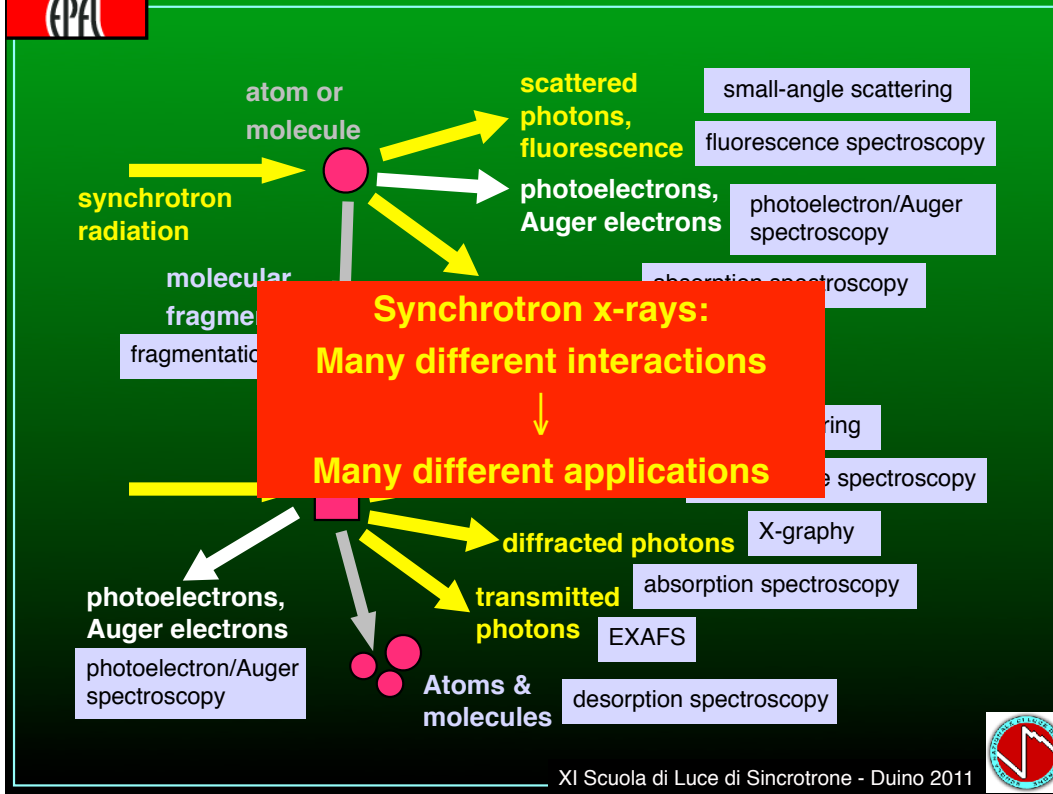


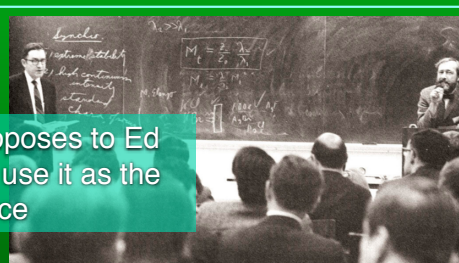
A real synchrotron facility: Diamond (UK)



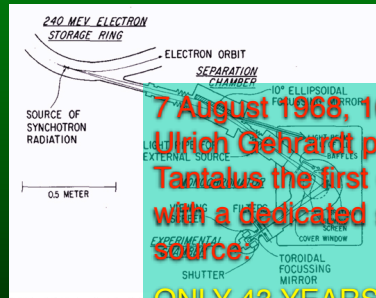
Why x-rays and ultraviolet?







1966: Fred Brown (Urbana) proposes to Ed Rowe, the father of Tantalus, to use it as the first dedicated synchrotron source



7 August 1968, 10:40 a.m.:
Ulrich Genrard performs on
Tantalus the first experiment
with a dedicated synchrotron
source.
ONLY 43 YEARS AGO!!!



Synchrotron and Free Electron Laser Facilities in the World (2011):

64 in 27 Countries

(operating or under construction)

Historical Growth:

Worldwide ISI data 1968-2011,
Keywords: "synchrotron" or "free
electron laser"

1968: 64

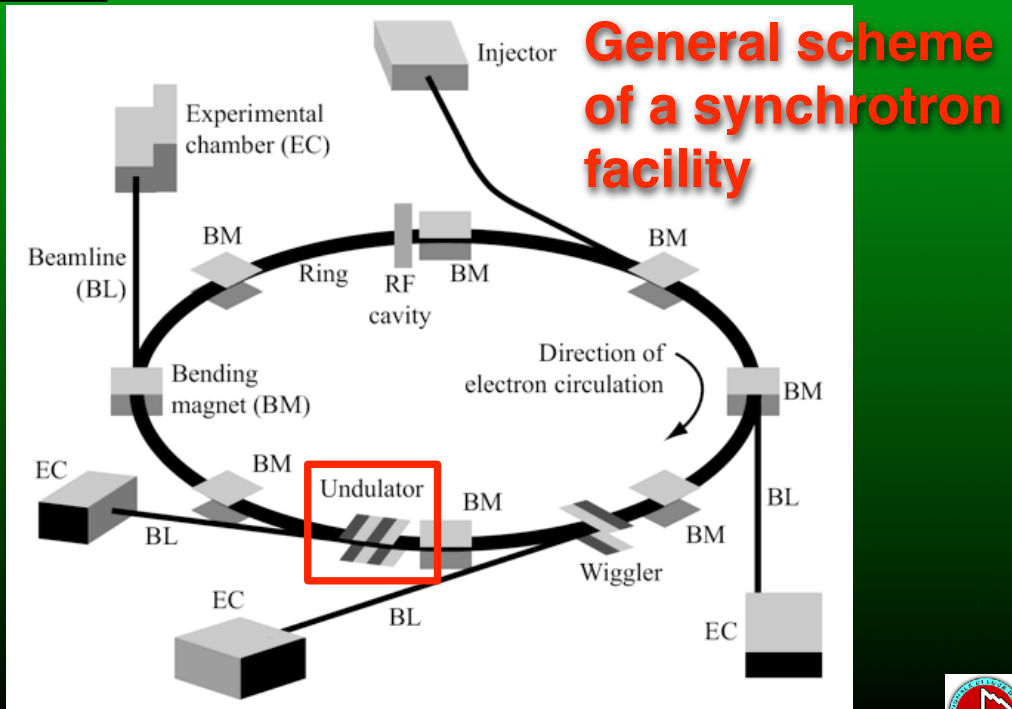
1980: 240

1990: 1,010

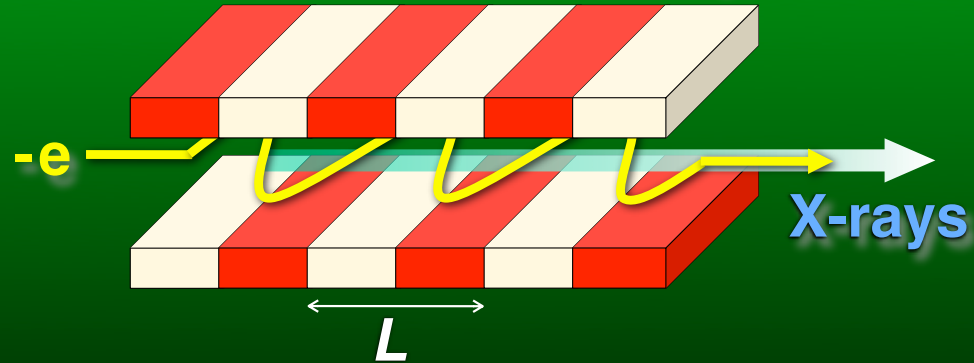
2000: 4,674

2010: 6,763





Why do the electrons in an undulator emit x-rays?



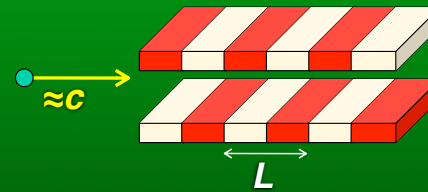
That is a puzzle: the typical undulator period, L , is of the order of **centimeters** -- whereas the x-ray wavelengths are of the order of **Angstroms!!!**

The key to understand: **Einstein's relativity** -- with its factor $\gamma = (1 - u^2/c^2)^{-1/2}$ (order of magnitude: 10^3 - 10^4)



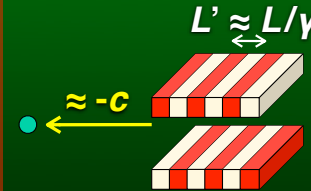
So, why short x-ray wavelengths?

The wiggler point of view: an electron arrives at a speed $u \approx c$



The electron point of view:

- A **periodic transverse B-field** arrives at speed $\approx -c$
- Its Lorentz transformation is a transverse **B-field plus a transverse E-field** perpendicular to it.
- The period L is **Lorentz-contracted** to $L' \approx L/\gamma$
- Thus, the electron “sees” the wiggler like a photon wave with wavelength $\approx L/\gamma$



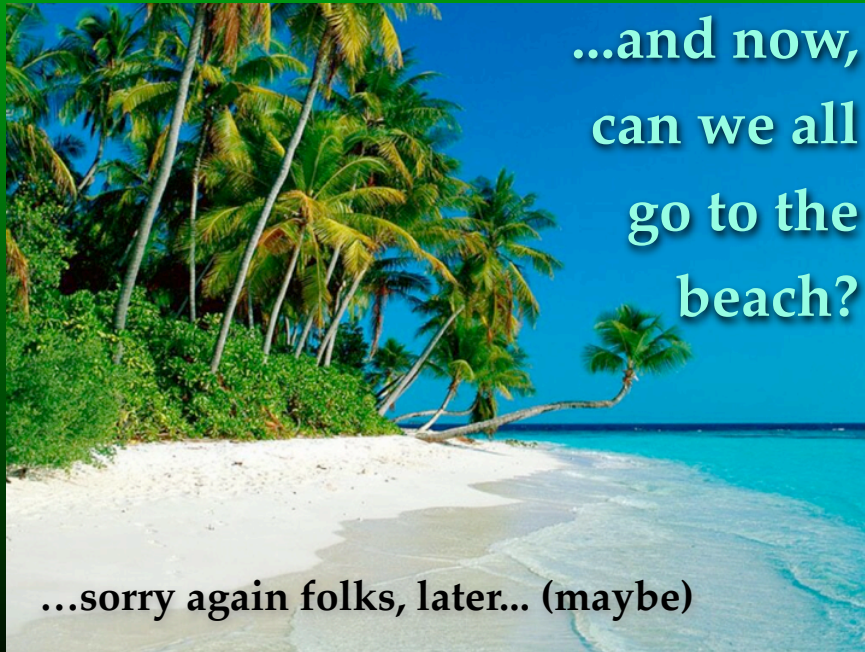
- The electron **scatters this “wave”**: this is the cause of its photon emission.
- The wavelength in the laboratory frame is **Doppler-shifted** by $\approx 2\gamma$, becoming $\lambda \approx L/2\gamma^2$
- Since γ is very large, λ corresponds to **x-rays!**



In summary, what produces the high brightness of a real synchrotron source?

- Free electrons can emit more power than bound electrons --> **high flux**
- The control of the electron beam trajectories in the storage ring is very sophisticated: small transverse beam cross section --> **small photon source size**
- Relativity drastically **reduces the angular divergence** of the emitted synchrotron radiation



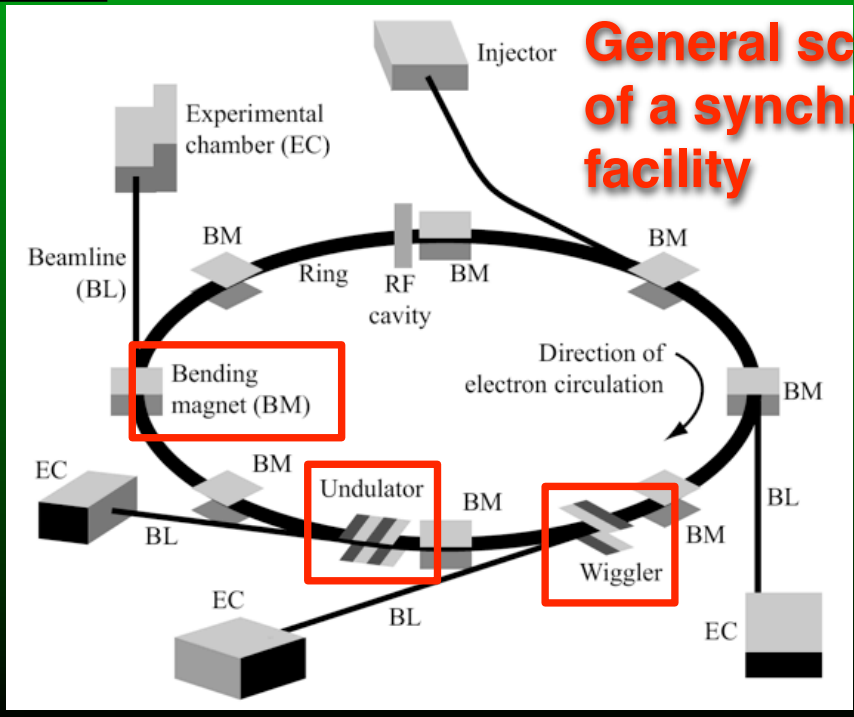


...and now,
can we all
go to the
beach?

...sorry again folks, later... (maybe)

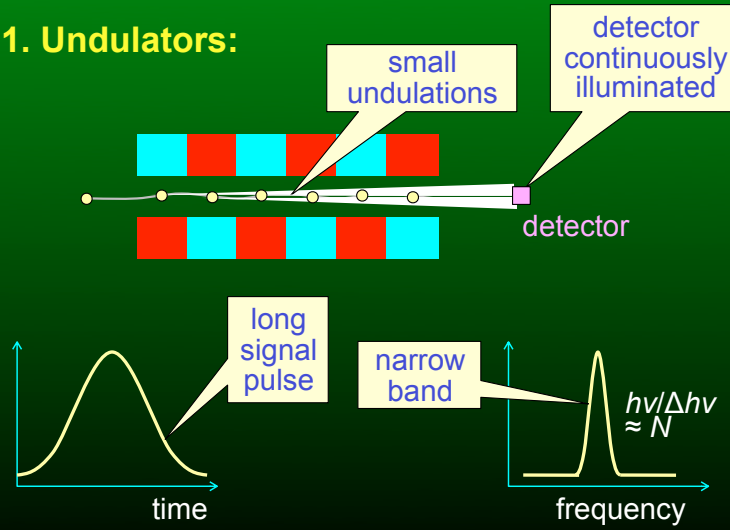


General scheme of a synchrotron facility



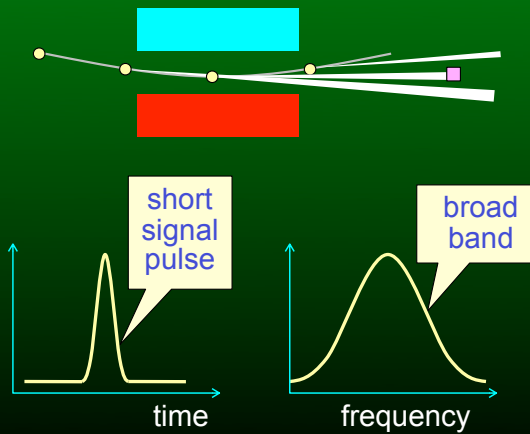
3 types of sources:

1. Undulators:



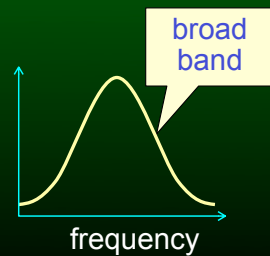
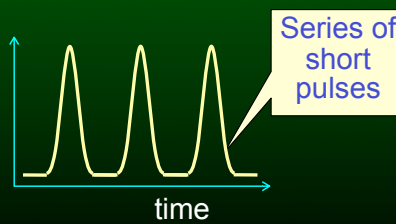
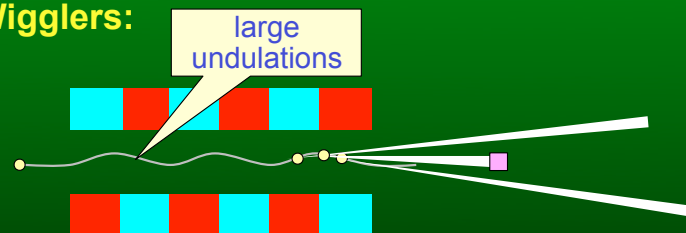
3 types of sources:

2. Bending magnets:

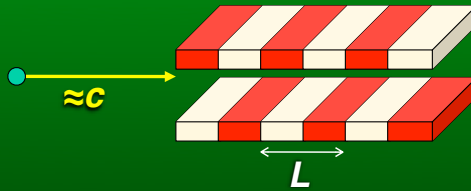


3 types of sources:

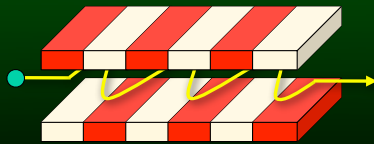
3. Wigglers:



Controlling the undulator wavelength:



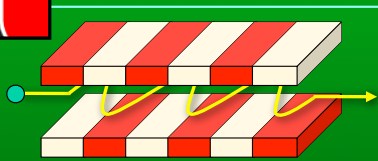
Starting point: we have seen that $\lambda \approx \lambda_0 = L/2\gamma^2$, so λ could be changed by changing γ (i.e., the electron energy)



Plus: the electron oscillations and the transverse velocity are proportional to the wiggler B -field. The Lorentz force does no work so the kinetic energy is constant: as the transverse velocity increases, the longitudinal velocity u decreases.

This effectively changes $\gamma = (1-u^2/c^2)^{-1/2}$, so that λ can be modified by tuning B .





Controlling the x-ray wavelength (continues):

In detail:

- The transverse velocity v_T is proportional to the B-field strength B
- The kinetic energy stays constant, so the longitudinal speed squared changes from u^2 to $(u^2 - v_T^2)$
- This effectively changes $1/\gamma^2$ from $(1 - u^2/c^2)$ to $(1 - u^2/c^2 - v_T^2/c^2)$
- And λ changes from $\lambda_0 \approx (L/2)(1 - u^2/c^2)$ to $\lambda \approx \lambda_0(1 - K^2/2)$, where K^2 is proportional to B^2

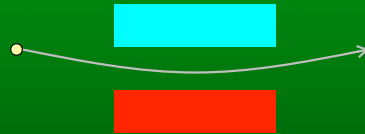
Note: this is the "central" emitted wavelength -- there is a wavelength band $\Delta\lambda$ around it

In fact:

- An electron going through an undulator with N_w periods emits a train of N_u wavelengths, with length $N_w\lambda$ and duration $\Delta t = N_w\lambda/c$
- Fourier transform (frequency): $\Delta\nu = c/N_w\lambda = \nu/N_w$
- $\Delta\lambda/\lambda = \Delta\nu/\nu = 1/N_w$

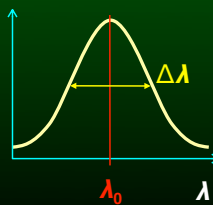
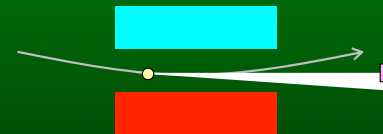


Bending magnet emission spectrum:

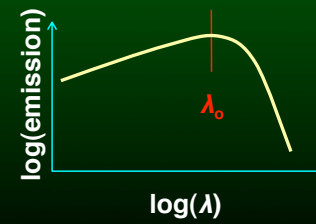


The (relativistic) rotation frequency of the electron determines the (Doppler-shifted) central wavelength:
 $\lambda_0 = (1/2\gamma^2)(2\pi cm_0/e)(1/B)$

The "sweep time" δt of the emitted light cone determines the frequency spread $\delta \nu$ and the wavelength bandwidth:
 $\Delta\lambda / \lambda_0 = 1$

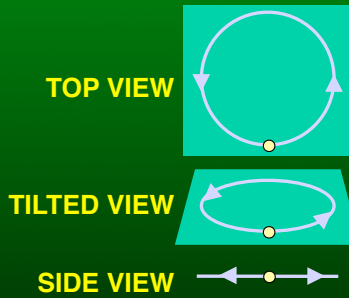


A peak centered at λ_0 with width $\Delta\lambda$: is this really the well-known synchrotron spectrum?
YES -- see the log-log plot:



Synchrotron light polarization:

Electron in a storage ring:



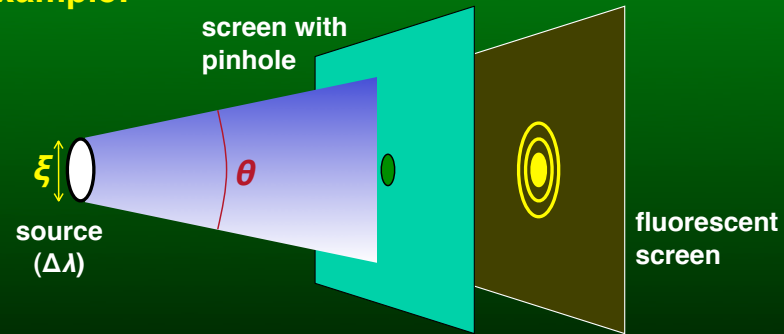
Polarization:
Linear in the plane of the ring,
elliptical out of the plane

Special (elliptical) wigglers and undulators can provide elliptically polarized light with high intensity



Coherence: “the property that enables a wave to produce **visible** diffraction and interference effects”

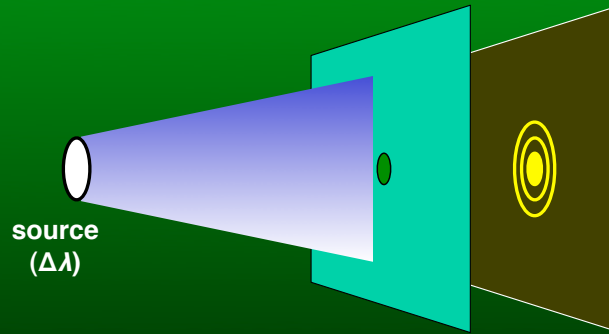
Example:



The diffraction pattern may or may not be visible on the fluorescent screen depending on the source size ξ , on its angular divergence θ and on its wavelength bandwidth $\Delta\lambda$



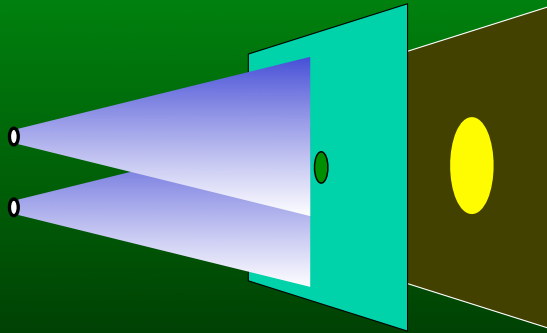
Longitudinal (time) coherence:



- Condition to see the pattern: $\Delta\lambda/\lambda < 1$
- Parameter characterizing the longitudinal coherence:
“coherence length”: $L_c = \lambda^2/\Delta\lambda$
- Condition of longitudinal coherence: $L_c > \lambda$



Lateral (space) coherence — analyzed with a source formed by two point sources:



- Two point sources produce overlapping patterns: diffraction effects may no longer be visible.
- However, if the two source are close to each other an overall diffraction pattern may still be visible: the condition is to have a **large “coherent power”** $\approx (\lambda \xi \theta)^2$

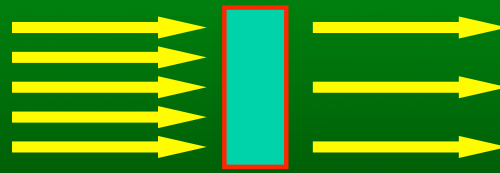


Coherence — summary:

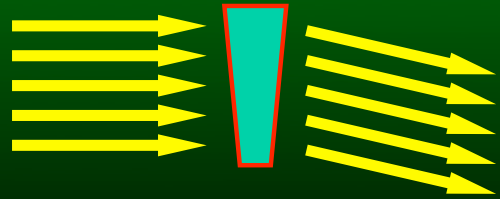
- Coherence in general requires a large coherence volume $L^2\lambda^4/(\xi^2\Delta\lambda) = L_c (L^2\lambda^2/\xi^2)$
- Longitudinal coherence: requires a large coherence length $L_c = \lambda^2/\Delta\lambda$
- Lateral coherence: requires a large coherent power $\approx (\lambda\xi\theta)^2$
- **Both difficult to achieve for small wavelengths (x-rays)**
- The geometric conditions for large $(\lambda\xi\theta)^2$ are **the same as for high brightness**



Light-matter Interactions in Radiology:



Absorption -- described by the absorption coefficient α

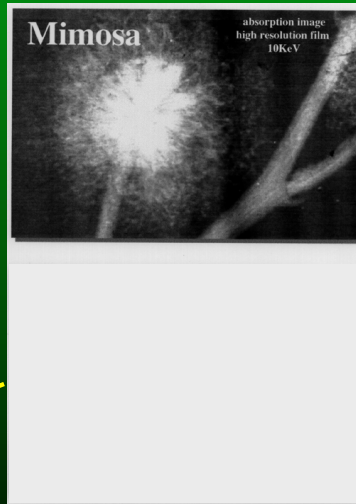


Refraction (and diffraction/interference) -- described by the refractive index n

For over one century, radiology was based on absorption: why not on refraction /diffraction?



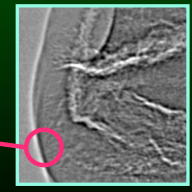
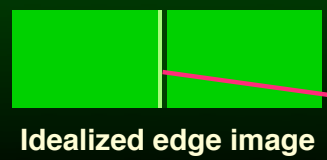
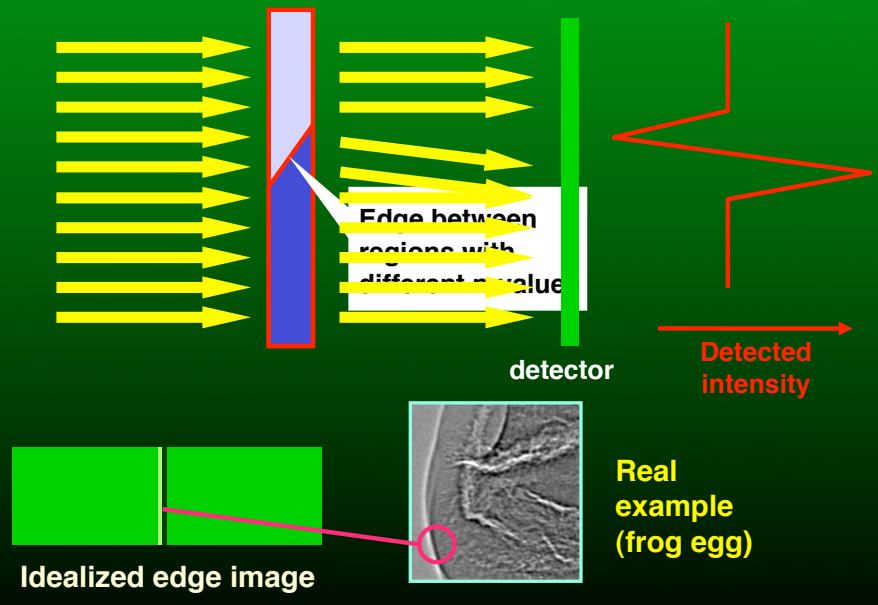
Conventional radiology



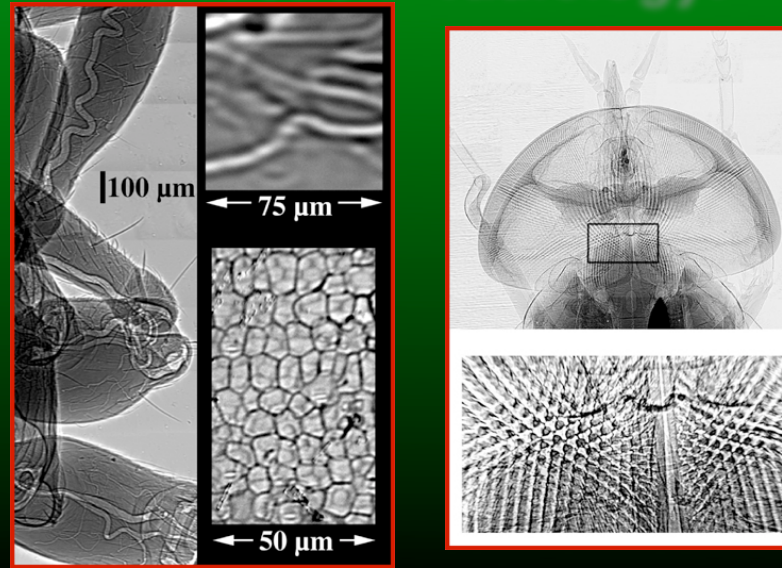
Refractive-index radiology (Giuliana Tromba)



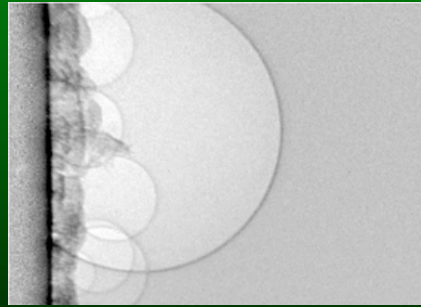
“Refraction” x-ray imaging:



Examples of “refraction” radiology:



Building on bubbles (zinc electrodeposition):



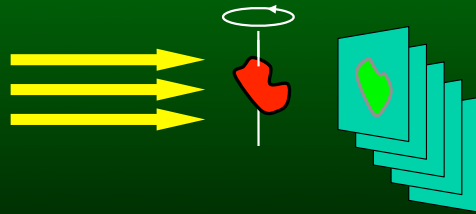
↑ substrate
↑ overlayer
↑ gas bubbles
↑ solution



X-ray (micro)tomography:

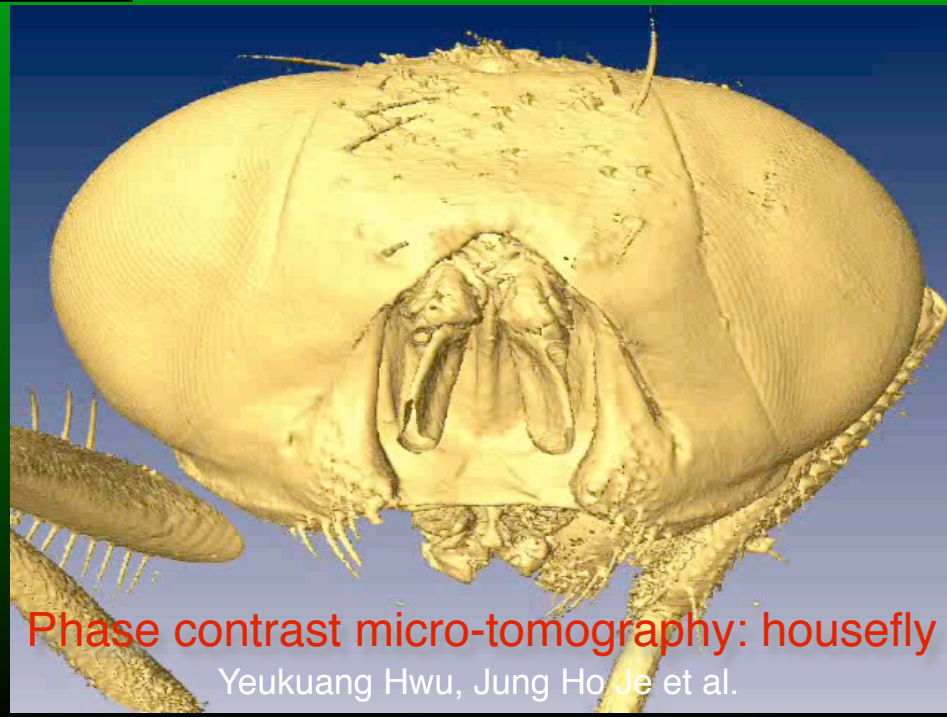


A single (projection) x-ray image does not deliver three-dimensional information



In tomography, many x-ray images taken at different angles are processed to obtain different views of the object in three dimensions -- for examples "slices"





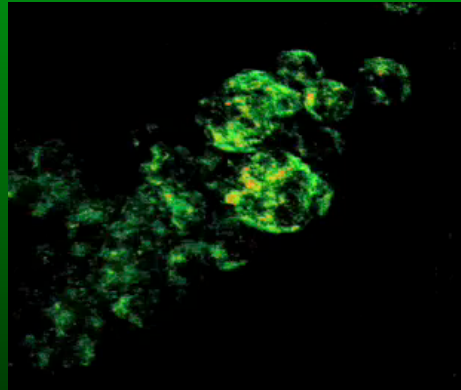
Phase contrast micro-tomography: housefly

Yeukuang Hwu, Jung Ho Je et al.



From detection to treatment?

Y. S. Chu, J. M. Yi, F. De
Carlo, Q. Shen, W.-K-
Lee, H. J. Wu, C. L.
Wang, J. Y. Wang, C. J.
Liu, C. H. Wang, S. R.
Wu, C. C. Chien, Y. Hwu,
A. Tkachuk, W. Yun, M.
Feser, K. S. Liang, C. S.
Yang, J. H. Je, G.
Margaritondo



**Agglomerated Au nanoparticles
attached to cancer cells**



New types of sources:

- **Ultrabright storage rings (SLS, new Grenoble project) approaching the diffraction limit**
- **X-ray and Ultraviolet X-ray free electron lasers (FEL's)**
- **Energy-recovery machines**
- **Inverse-Compton-scattering table-top sources**





April 21, 2009 - New Era of Research Begins as World's First Hard X-ray Laser Achieves "First Light"

X-ray laser pulses of unprecedented energy and brilliance produced at SLAC



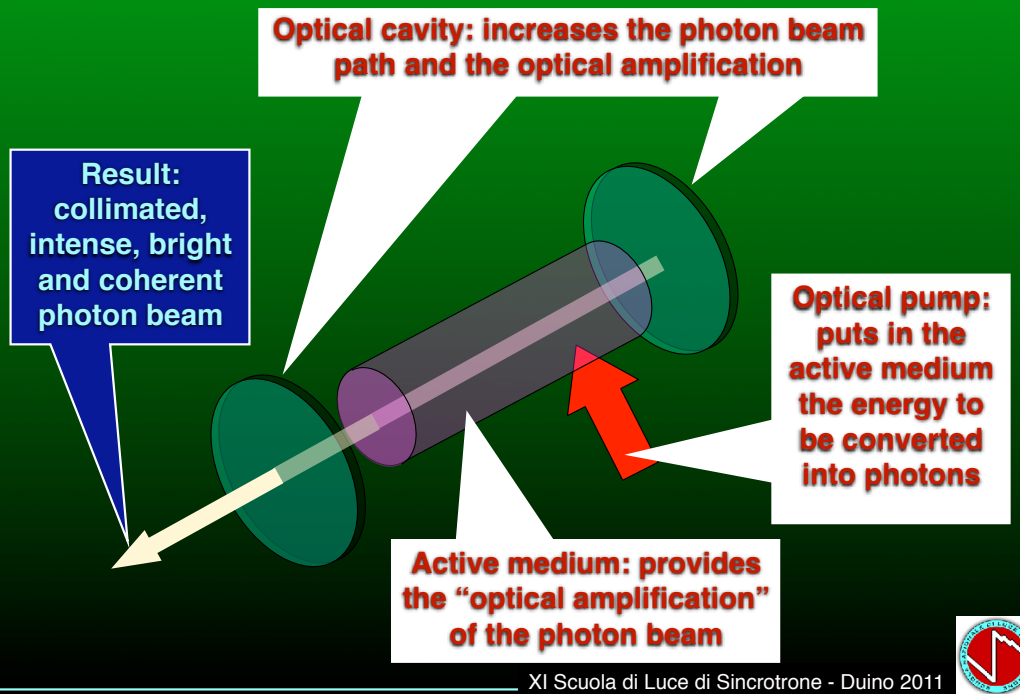
**Claudio Pellegrini,
UCLA – leader of
the X-FEL theory**



**John Made,
inventor of
the FEL**



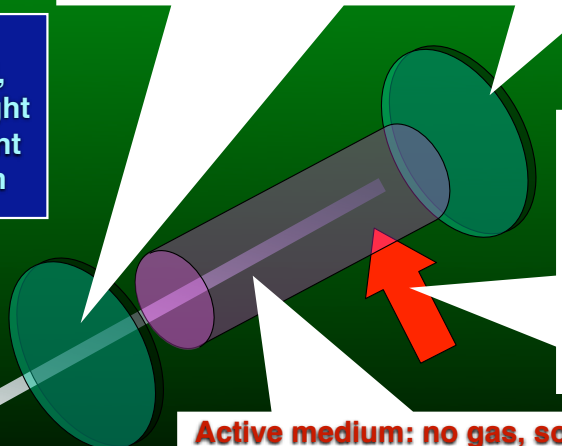
The ingredients of a normal lasers:



Normal lasers ----> x-ray laser:

No x-ray mirrors --> no optical cavity --> enough amplification needed for one-pass lasing

**Result:
collimated,
intense, bright
and coherent
x-ray beam**



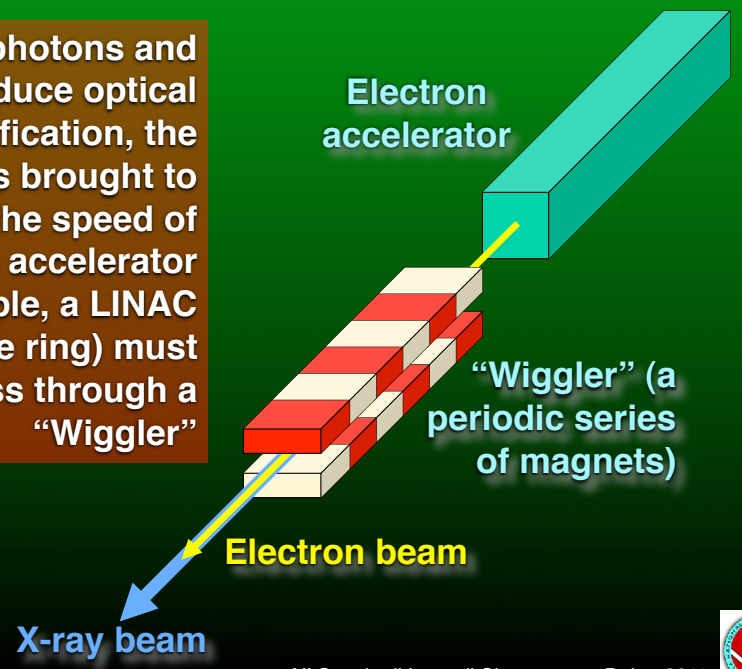
**Optical pump:
the free
electrons
provide the
energy and
transfer it to
the photons**

**Active medium: no gas, solid or liquid
but "free electrons" in an accelerator:
hight power possible without damage**

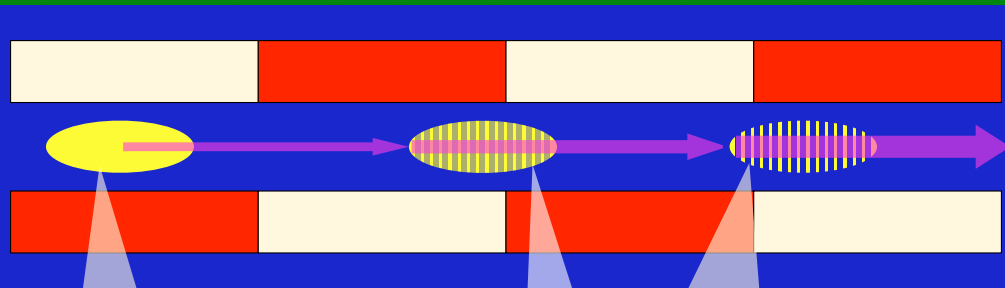


Free-electron lasers (FEL's):

To emit photons and produce optical amplification, the electrons brought to (almost) the speed of light by an accelerator (for example, a LINAC or a storage ring) must pass through a "Wiggler"



This is what happens in detail:



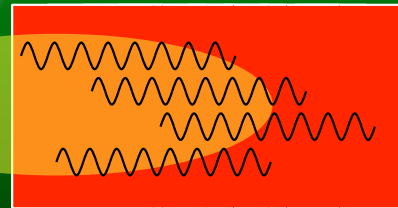
A bunch of electrons enters the wiggler: some of them stochastically start emitting waves

The combined wiggler+wave action progressively microbunches the electrons. The emission of microbunched electrons enhances the previously emitted waves

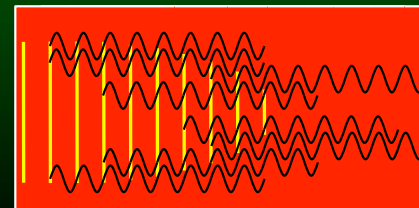
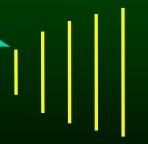


Microbunching makes the difference: this is what happens from the electron point of view:

With no microbunching, as electrons enter the **wiggler**, they emit in an uncorrelated way

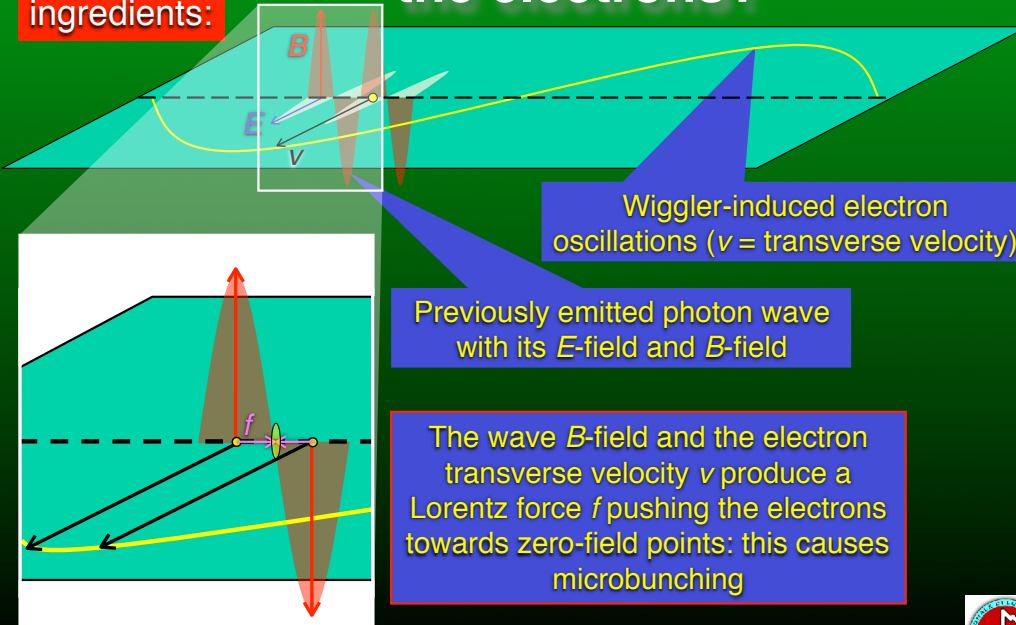


Instead, the electrons in the wiggler-induced microbunches emit in a correlated way, enhancing previously emitted waves



What microbunches the electrons?

Two key ingredients:

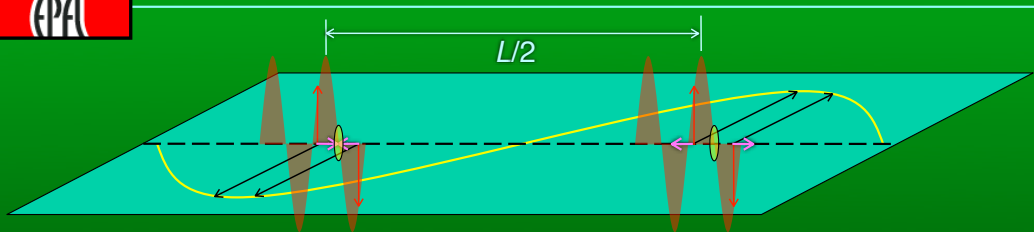


Wiggler-induced electron oscillations ($v =$ transverse velocity)

Previously emitted photon wave with its E -field and B -field

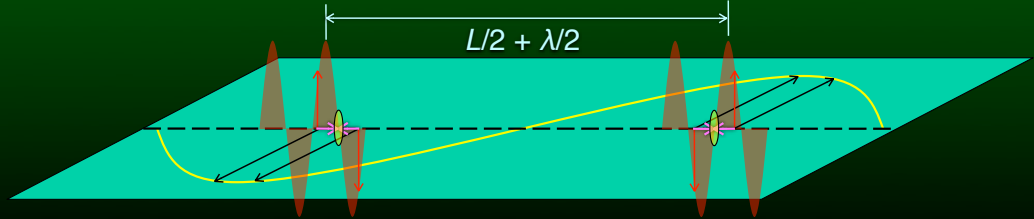
The wave B -field and the electron transverse velocity v produce a Lorentz force f pushing the electrons towards zero-field points: this causes microbunching





...but something seems wrong: after 1/2 wiggler period, the electron transverse velocity is reversed. If the wave travels together with the electron, the B -field stays the same. Are the forces and the microbunching reversed?

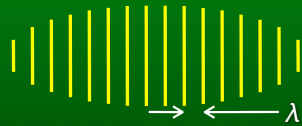
No! Electron and wave do not travel together: the electron speed is $u < c$. As the electron travels over $L/2$ in a time $L/(2u)$, the wave travels over $[L/(2u)]c$. The difference is $(L/2)(c/u - 1) \approx L/(4\gamma^2) = \text{half wavelength}$



the forces are not reversed, microbunching continues



Why is microbunching (and lasing) more difficult for x-rays than for longer wavelengths?

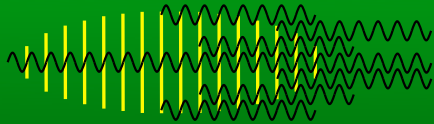


On one hand, at short wavelengths the microbunches are closer to each other and this facilitates microbunching

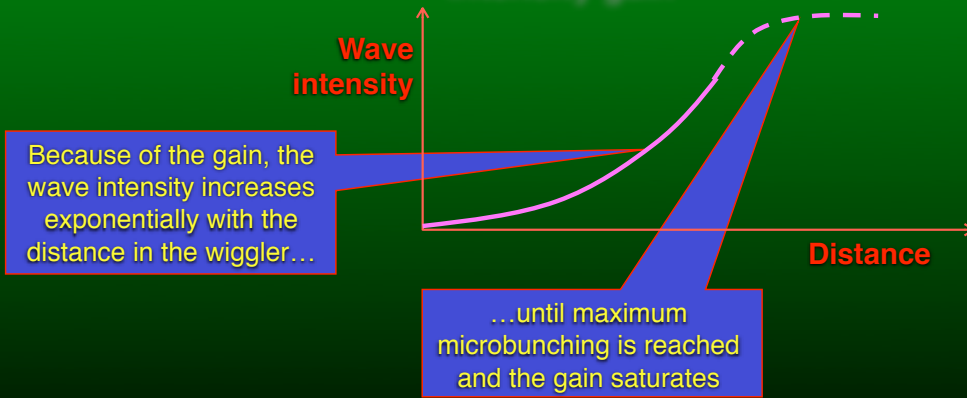
But:

- Short wavelengths require a high electron energy corresponding to a large γ - factor
- The large γ makes the electrons “heavy” and therefore difficult to move towards microbunches: their **transverse** relativistic mass is γm_0 and the **longitudinal** relativistic mass (directly active in the microbunching mechanism) is $\gamma^3 m_0$
- This offsets the advantage of closer microbunches, making microbunching difficult





Microbunching produces correlated emission proportional to the square of the number of electrons, and a wave intensity gain



Because of the gain, the wave intensity increases exponentially with the distance in the wiggler...

...until maximum microbunching is reached and the gain saturates

For an x-ray FEL (no 2-mirror cavity), gain saturation must be reached before the end of the (very long) wiggler, in a single pass

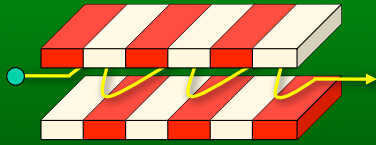


Why the exponential intensity increase?

- The total energy transfer rate from the electron beam to a pre-existing wave of intensity I is determined by two factors: (1) the transfer rate for each single electron (2) the effects of microbunching
- The one-electron transfer rate is given by the (negative work) proportional to $E v$, where E = the wave (transverse) E-field and v = the electron transverse velocity.
- But E is proportional to $I^{1/2}$ so the energy transfer rate for one electron is proportional to $I^{1/2}$
- The effects of microbunching are proportional to the Lorentz force that causes it, which is produced by v_T and by the B-field B of the pre-existing wave. Since B is proportional to $I^{1/2}$, they give another factor $I^{1/2}$
- Overall, dI/dt is proportional to $I^{1/2} I^{1/2} = I$
- This corresponds to an exponential increase as a function of t and therefore also of the distance = ut



An FEL emits very short pulses:



The basic physics -- we have seen that:

- One electron emits a wave train of length $N_w \lambda$
- The duration of this train is $N_w \lambda / c$

Take for example $N_w = 3 \times 10^3$ and $\lambda = 10$ angstrom: the duration is 10^{-16} s = 0.1 femtoseconds

- The real pulse duration and time structure are determined by the length and shape of the electron bunches and by other factors in the wave emission process
- But the real pulse duration can still reach the femtosecond range



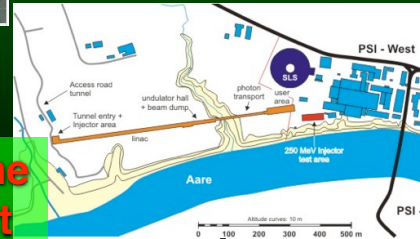
The FERMI X-FEL at Elettra, Trieste



The European X-FEL project underway at DESY, Hamburg



The Swiss X-FEL at the Paul-Scherrer Institut



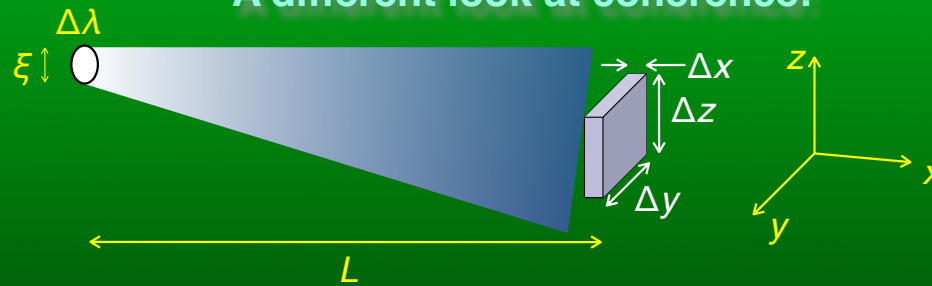
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A different look at coherence:



A source of size ξ and bandwidth $\Delta\lambda$ can illuminate coherently a volume $\Delta x \Delta y \Delta z$ at the distance L . Let us see what is this coherence volume.

Along x : if two waves of wavelength λ and $\lambda + \Delta\lambda$ are in phase at a certain time, they will be out of phase after Δt such that $\Delta\omega\Delta t = 2\pi$ or $\Delta t = 2\pi/\Delta\omega = \lambda^2/(c\Delta\lambda)$.

Thus, $\Delta x = c\Delta t = \lambda^2/\Delta\lambda = L_c$.

Along y : the spread in k -vector is $\Delta k = k\xi/L = 2\pi\xi/(L\lambda)$.

If two waves with k -vectors 0 and Δk along y are in phase at a certain point, they will be out of phase at a distance Δy such that $\Delta k\Delta y = 2\pi$ or $\Delta y = L\lambda/\xi$.

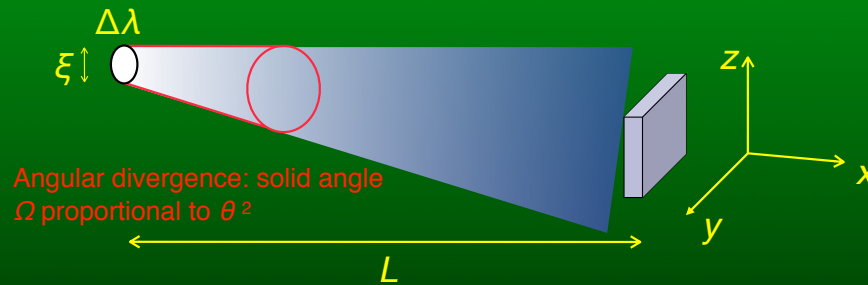
Along z : same as along y .

Coherence volume: $\Delta x \Delta y \Delta z = L^2 \lambda^4 / (\xi^2 \Delta\lambda)$

Behind this: Heisenberg! Photons in the coherence volume cannot be distinguished from each other



This also explains the notion of “coherent power”:



The solid angle corresponding to the area $\Delta y \Delta z$ is $\Delta y \Delta z / L^2$.

If the solid angle of the emitted light is $\approx \theta^2$, then only a portion $(\Delta y \Delta z / L^2) / \theta^2$ of the total emitted power illuminates the coherence volume.

This is the **coherent power**.

Since $\Delta y \Delta z = (L \lambda \xi)^2$, the coherent power equals $\approx (\lambda \xi \theta)^2$.

